

## Physical Quantities and Units.

\* Any quantity that can be measured and has unit is called a physical quantity.

\* Physical Quantities are divided into 2 types.

1) Base Quantities.

2) Derived Quantities.

A Base quantity is one which cannot be expressed using other physical quantities examples of Base quantities

Base quantities

Base units.

length

m

time

s

temperature

K / °C

mass

kg

amount of substance

mol

Current

A

light intensity

cd (Candela)

\* A derived quantity is one which can be expressed using one or more base quantities. Examples are

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Area	$m^2$
Volume	$m^3$
density	$kg\,m^{-3}$
speed	$m/s$
Acceleration	$m\,s^{-2}$
Force	$N$

Force Base units:

$$F = m a$$

$$= kg \cdot m\,s^{-2} \quad \text{Base unit}$$

$$P = \frac{F}{A}$$

$$\frac{kg\,m\,s^{-2}}{m^2} \Rightarrow kg\,m^{-1}\,s^{-2}$$

Work done

$$W = F \times d$$

$$kg\,m\,s^{-2} \times m$$

$$kg\,m^2\,s^{-2}$$

Power

$$P = \frac{W}{t} = \frac{kg\,m^2\,s^{-2}}{s} = kg\,m^2\,s^{-3}$$

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$$\text{Energy} = \text{J}$$

$$\text{WD} = \text{J}$$

\* Energy will have same base units as W. done.

### Charge

$$Q = I t$$

$$\text{A} \cdot \text{s}$$

 $\Rightarrow$ 

$$\boxed{\text{A s}}$$

Q = Charge

I = current.

t = time.

$$\text{Voltage} = \frac{\text{WD}}{Q}$$

$$= \frac{\text{kg m}^2 \text{s}^{-2}}{\text{A s}}$$

$$\boxed{\text{kg A}^{-1} \text{m}^2 \text{s}^{-3}}$$

$$\text{Resistance} = \frac{V}{I}$$

$$\frac{\text{kg A}^{-1} \text{m}^2 \text{s}^{-3}}{\text{A}}$$

 $\Rightarrow$ 

$$\boxed{\text{kg m}^2 \text{A}^{-2} \text{s}^{-3}}$$

### Specific heat Capacity

$$Q = mc \Delta Q$$

$$c = \frac{Q}{m \cdot \Delta T} = \frac{\text{kg m}^2 \text{s}^{-2}}{\text{kg} \cdot \text{K}} = \text{m}^2 \text{s}^{-2} \text{K}^{-1}$$



## Specific Latent Heat

$$Q = ml$$

$$l = \frac{Q}{m} = \frac{\text{kg m}^2 \text{s}^{-2}}{\text{kg}} \quad \boxed{\text{m}^2 \text{s}^{-2}}$$

$$Q) \quad F = \frac{Q^2}{4\pi \epsilon r^2} \quad F = \frac{\gamma I^2}{2\pi \cdot d}$$

Write down base  
units of  $\frac{1}{\epsilon}$  ?

Equate:

$$\frac{Q^2}{4\pi \epsilon r^2} = \frac{\gamma \cdot I^2}{2\pi \cdot d}$$

$$\frac{1}{\epsilon} = \frac{I^2 \cdot 4\pi r^2}{2\pi \cdot d \times Q^2}$$

$$= \frac{2 \times r^2 \times I^2}{Q^2 \times d}$$

$$= \frac{2 \times \text{m}^2 \times \text{A}^2}{(\text{As})^2 \times \text{m}}$$

$\Rightarrow$

$$\boxed{\text{m s}^{-2}}$$

$F$  = force

$Q$  = charge

$I$  = current

$d$  = distance

$r$  = radius

Remember constants  
have no units hence  
such quantities are  
called dimensionless  
quantities.



## Homogeneity of Physical Equation

An Equation is said to be homogenous if base units on LHS are identical to the base units on RHS.

(for eg)

For any equation to be classified as a correct Equation, it must satisfy the test of homogeneity.

$$1) \quad d = s \times t$$

$$m = (ms^{-1}) (s)$$

$$m = m \quad [\text{hence homogenous}]$$

$$2) \quad v = f \lambda$$

$$ms^{-1} = s^{-1} m$$

$$ms^{-1} = ms^{-1} \quad [\text{hence homogenous}]$$

$$3) \quad P = \rho gh$$

$$kg \, m^{-1} s^{-2} = kg \, m^{-3} \times ms^{-2} \times m$$

$$= kg \, m^{-1} s^{-2}$$

$$[\text{hence homogenous}]$$

$$4) \quad v = u + at$$

⇒ If an equation contains more than one term on any one side, then for homogeneity firstly breakdown the equation.

\* Compare  $v$  with  $u$

$$ms^{-1} = ms^{-1}$$

\* Compare  $v$  with  $at$

$$ms^{-1} = ms^{-2} (s)$$

$$ms^{-1} = ms^{-1}$$

Hence now equation can be classified as correct equation.

Hence now the eq can be classified as correct or Homogeneous, Eq.

Q) In the following examples suggest which eq can be classified as correct/Homogenous equation?

i)  $E = mv$

ii)  $v = fg$

iii)  $E = \frac{1}{2} f v^3$

iv)  $v = \sqrt{g \lambda}$

$E = \text{Energy}$

$m = \text{mass}$

$v = \text{velocity}$

$f = \text{frequency}$

$g = \text{acceleration of free fall}$

$\lambda = \text{frequency}$

$\lambda = \text{Wave length.}$

Solution.

i)  $E = mv$

$$\text{kg m}^2 \text{s}^{-2} = (\text{kg})(\text{ms}^{-1})$$

Not Homogenous

ii)  $v = fg$

$$\text{ms}^{-1} = (\text{s}^{-1})(\text{ms}^{-2})$$

$$\text{ms}^{-1} = \text{ms}^{-3}$$

Not Homogenous

iii)  $E = \frac{1}{2} f v^3$

$$\text{kg m}^2 \text{s}^{-2} = \text{s}^{-1} (\text{ms}^{-1})^3$$

$$\text{kg m}^2 \text{s}^{-2} = \text{s}^{-1} \text{m}^3 \text{s}^{-3}$$

$$= \text{s}^{-4} \text{m}^3$$

Not Homogenous

iv)  $v = \sqrt{g \lambda}$

$$(\text{ms}^{-1})^2 = (\sqrt{\text{ms}^{-2} \text{m}})^2$$

$$\text{m}^2 \text{s}^{-2} = \text{m}^2 \text{s}^{-2}$$

Homogenous





Q) Given that the eq shown below is **homogenous** use this information to find the **base unit of P and Q**.

$$3 \left( L + \frac{a^2}{P} \right) = Q T^2 \sin Q$$

$L = \text{length}$

$a = \text{radius}$

$T = \text{time}$

Q) Given that the eq shown below is **homogenous** use this information to find the **base unit of P and Q**.

$$3 \left( L + \frac{a^2}{P} \right) = Q T^2 \sin Q$$

$$3L + \frac{3a^2}{P} = Q T^2 \sin Q$$

$$3L = Q T^2 \sin Q$$

$$\frac{m}{s^2} = Q$$

$$Q = m s^{-2}$$

$$\frac{3a^2}{P} = Q T^2 \sin Q$$

↓ ignore no units.

$$\frac{a^2}{Q T^2} = P \Rightarrow \frac{m^2}{m s^{-2} \times s^2} = \boxed{m}$$



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⇒ How to find unknown constants  $x, y, z$  etc in a Homogenous equation.

In the given eq find values of  $x, y$  &  $z$  given that equation is Homogenous.

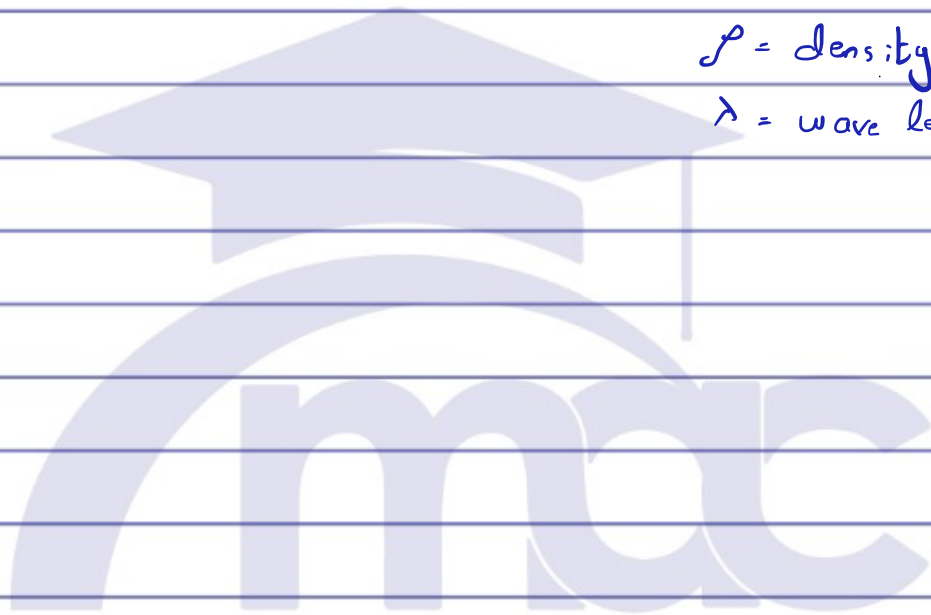
$$v = \lambda^x \rho^y \mu^z$$

$v$  = velocity

$\rho$  = pressure

$\mu$  = density.

$\lambda$  = wave length.



→ How to find unknown constants  $x, y, z$  etc in a Homogenous equation.

In the given eq find values of  $x, y$  &  $z$  given that equation is Homogenous.

$$v = \lambda^x \rho^y \mu^z$$

$$ms^{-1} = m^x (kgm^{-1}s^{-2})^y (kgm^{-3})^z$$

$v$  = velocity

$\rho$  = pressure

$\mu$  = density.

$\lambda$  = wave length.

i) Compare (m) from both sides.

$$m^1 = m^x (m^{-1})^y (m^{-3})^z$$

Use Indices.

$$1 = x - y - 3z \quad \text{--- (1)}$$

ii) Compare s

$$s^{-1} = (s^{-2})^y$$

Use Indices.

$$-1 = -2y$$

$$\frac{-1}{-2} = y$$

$$\frac{1}{2} = y$$

iii) Compare kg

$$kg^0 = kg^y kg^z$$

$$0 = y + z$$

$$z = -y$$

$$z = -\frac{1}{2}$$

For x.

$$x = 1 + y + 3z$$

$$x = 1 + \frac{1}{2} + 3\left(-\frac{1}{2}\right)$$

$$x = \frac{3}{2} - \frac{3}{2}$$

$$x = 0$$

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Question:

$$T = L^x g^y$$

$T$  = time

$L$  = length

$g$  = Acc due to gravity.

Question:

$$T = L^x g^y$$

$T$  = time

$L$  = length

$g$  = Acc due to gravity.

$$(s) = m^x (m s^{-2})^y$$

Compare powers of s

$$1 = -2y$$

$$y = \frac{-1}{2}$$

Compare powers of m

$$0 = x + y$$

$$x = \frac{1}{2}$$

$$0 = x - \frac{1}{2}$$



Question:

$$F = 6\pi r n v$$

F = Force

i) Find Base unit of n.

r = radius

v = velocity

$$\text{ii) } \frac{V}{t} = (L)^x \left( \frac{P}{r} \right)^y (n)^z$$

Using your answer in Part (i) find x y and z

V = Volume t = time L = length r = radius P = Pressure

Question:

$$F = 6\pi r n v$$

F = Force

i)

r = radius

v = velocity

$$\text{kg m s}^{-2} = n (\text{ms}^{-1})$$

$$\frac{\text{kg m s}^{-2}}{\text{m s}^{-1}} = n$$

$$\boxed{\text{kg m}^{-1} \text{s}^{-1} = n}$$

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$$ii) \frac{V}{t} = (L) \left( \frac{P}{r} \right)^y (n)^z$$

Using your answer in Part (i) find  $x$ ,  $y$  and  $z$

$V$  = Volume     $t$  = time     $L$  = length     $r$  = radius     $P$  = Pressure

$$\frac{m^3}{s} = (m)^x \left( \frac{kg m^{-1} s^{-2}}{m} \right)^y (kg m^{-1} s^{-2})^z$$

$$m^3 s^{-1} = m^x (kg m^{-2} s^{-2})^y (kg m^{-1} s^{-2})^z$$

i) Compare "s"

$$-1 = -2y - 2 \quad \text{--- (1)}$$

ii) Compare "kg"

$$0 = y + z \quad \text{--- (2)}$$

iii) Compare "m"

$$3 = x - 2y - 2 \quad \text{--- (3)}$$

$$z = -y$$

$$-1 = -2y - (-y)$$

$$-1 = -2y + y \Rightarrow$$

$$-1 = -y$$

$$y = 1$$

$$z = -1$$

$$x = 4$$



## Question

$$I = S q n v^x$$

Find  $x$  :

$I$  = current

$S$  = Area

$q$  = charge

$v$  = velocity

$n$  = no of electrons per unit  
Volume

## Question

$$I = S q n v^x$$

Find  $x$  :

$$I = A \quad S = m^2 \quad q = As \quad n = \frac{1}{m^3}$$

$v = ms^{-1}$

$I$  = current

$S$  = Area

$q$  = charge

$v$  = velocity

$n$  = no of electrons per unit  
Volume

$$\frac{\text{number of electron}}{\text{Volume}} = \frac{1}{m^3}$$

$$A = (m^2) (As) (m^{-3}) (ms^{-1})^x$$

Concept

no of cows  
no of apples  
no of people

} No units

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⇒ Compare "m"

$$0 = 2 - 3 + x$$

$$x = -2 + 3$$

$$x = 1$$

lets compare "s"

$$0 = 1 - x$$

$$x = 1$$





⇒ Guys Must learn this by Next class

- Mass of an Apple = 200g to 400g
- Number of joules in 1 kwh =  $1000W \times 3600s = 3.6 \times 10^6 J$
- Wavelength of Red light = 700nm  
Wave length of Green light = 500nm  
Wavelength of Violet light = 400nm
- Pressure due to 10m of water =  $pgh = (1000)(10)(10) = 10^5 \text{ Pa}$
- Speed of sound in Air = 300m/s to 330m/s
- Density of Air =  $1.4 \text{ kg/m}^3$
- Mass of a protector = 20g to 50g
- Volume of an adults head (assume sphere apply  $\frac{4}{3} \times \pi r^3$  taking  $r \gg 8 \text{ cm}$ )
- Freq of audible sound = 20Hz to 20,000 Hz
- Wavelength of Ultraviolet = 10nm to 400nm
- Mass of 30cm plastic ruler = 30g to 100g
- Size (diameter) of a nucleus =  $10^{-13} \text{ m}$  to  $10^{-15} \text{ m}$
- Size (diameter) of an atom =  $10^{-9} \text{ m}$  to  $10^{-11} \text{ m}$
- Mass of a person = 70kg
- Height of a person = 1.5m
- Walking Speed of a person = 1.5m/s
- Speed of Car on motorway = 30m/s
- Volume of a can of drink =  $300 \text{ cm}^3$
- Density of water =  $1000 \text{ kg/m}^3$
- Density of Mercury =  $13600 \text{ kg/m}^3$
- Typical current in domestic appliance = 13A
- emf of a Car battery = 12V
- Average K.Energy of an athlete during a 100m race = 4000J
- Temperature of a hot oven =  $800^\circ \text{C}$

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PREFIX	POWER OF 10	SYMBOL
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pico	$10^{-12}$	p
------	------------	---

nano	$10^{-9}$	n
------	-----------	---

micro	$10^{-6}$	$\mu$
-------	-----------	-------

milli	$10^{-3}$	m
-------	-----------	---

centi	$10^{-2}$	c
-------	-----------	---

deci	$10^{-1}$	d
------	-----------	---

deka	$10^1$	da
------	--------	----

hecto	$10^2$	h
-------	--------	---

kilo	$10^3$	k
------	--------	---

mega	$10^6$	M
------	--------	---

giga	$10^9$	G
------	--------	---

tera	$10^{12}$	T
------	-----------	---

4) The momentum of an object of mass  $m$  is  $p$ . where  $p$

Which quantity has the same base units as  $\frac{p^2}{m}$ ?

- A energy
- B force
- C power
- D velocity

9) Which of the following definitions is correct and uses only quantities rather than units?

- A Density is mass per cubic metre.
- B Potential difference is energy per unit current.
- C Pressure is force per unit area.
- D Speed is distance travelled per second.

10) When a beam of light is incident on a surface, it delivers energy to the surface. The intensity of the beam is defined as the energy delivered per unit area per unit time.

What is the unit of intensity, expressed in SI base units?

- A  $\text{kg m}^{-2} \text{s}^{-1}$
- B  $\text{kg m}^2 \text{s}^{-3}$
- C  $\text{kg s}^{-2}$
- D  $\text{kg s}^{-3}$

12) A metal sphere of radius  $r$  is dropped into a tank of water. As it sinks at speed  $v$ , it experiences a drag force  $F$  given by  $F = krv$ , where  $k$  is a constant.

What are the SI base units of  $k$ ?

- A  $\text{kg m}^2 \text{s}^{-1}$
- B  $\text{kg m}^{-2} \text{s}^{-2}$
- C  $\text{kg m}^{-1} \text{s}^{-1}$
- D  $\text{kg m s}^{-2}$

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the expressions below

$a$  is acceleration,

$F$  is force,

$m$  is mass,

$t$  is time,

$v$  is velocity.

Which expression represents energy?

A  $Ft$

B  $Fvt$

C  $\frac{2mv}{t}$

D  $\frac{mt^2}{2}$

20) Which is



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